

1 Modeling of plasma-controlled evaporation and surface condensation 2 of Al induced by 1.06 and 0.248 μm laser radiations

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8 Phase transition on the surface of an aluminum target and vapor plasma induced by laser irradiation
9 in the nanosecond regime at the wavelengths of 1.06 μm in the infrared range and 0.248 μm in the
10 ultraviolet range with an intensity of 10^8 – 10^9 W/cm^2 in vacuum are analyzed. Special attention is
11 paid to the wavelength dependence of the observed phenomena and the non-one-dimensional effects
12 caused by the nonuniform (Gaussian) laser intensity distribution and the lateral expansion of the
13 plasma plume. A transient two-dimensional model is used which includes conductive heat transfer
14 in the condensed phase, radiative gas dynamics, and laser radiation transfer in the plasma as well as
15 surface evaporation and back condensation at the phase interface. It was shown that distinctions in
16 phase transition dynamics for the 1.06 and 0.248 μm radiations result from essentially different
17 characteristics of the laser-induced plasmas. For the 1.06 μm radiation, evaporation stops after the
18 formation of hot optically thick plasma, can occasionally resume at a later stage of the pulse, and
19 proceeds nonuniformly in the spot area, and the major contribution to the mass removal occurs in
20 the outer part of the irradiated region. Plasma induced by the 0.248 μm laser is colder and partially
21 transparent since it transmits 30%–70% of the incident radiation; therefore evaporation does not
22 stop but continues in the subsonic regime with the Mach number of about 0.1. The amount of
23 evaporated matter that condenses back to the surface is as high as 15%–20% and less than 10% for
24 the 1.06 and 0.248 μm radiations, respectively. For a beam radius smaller than ~ 100 μm , the
25 screening and retarding effect of the plasma weakens because of the lateral expansion, thickness of
26 the removed layer increases, and condensation after the end of the pulse is not observed.
27 Comparison of the numerical and experimental results on the removed layer thickness has shown,
28 in particular, the importance of accounting for the plasma effect to predict the correct trends for
29 radiation intensity and beam radius. © 2007 American Institute of Physics.
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32 I. INTRODUCTION

33 The technique of material removal from a condensed
34 target by the action of short high-power laser pulses usually
35 referred to as *laser ablation* (LA) forms the basis for a
36 number of technologies such as pulsed laser deposition
37 (PLD), micromachining, structuring, or analysis of solid
38 materials.^{1–4} Along with the intensity and the pulse duration,
39 the wavelength of laser radiation is a key parameter provid-
40 ing great flexibility to tailor this technique to suit specific
41 tasks. Fast progress in laser equipment as well as emergency
42 of advanced technologies have stimulated intensive studies
43 in this field over a long period of time.

44 For metal targets, surface evaporation is always an im-
45 portant mechanism of material removal.^{1,5} The process is
46 characterized by the formation of a sharp phase boundary
47 between the condensed and vapor phases and of a transient
48 nonequilibrium layer adjacent to the boundary referred to as
49 the Knudsen layer (KL). For equations of continuum me-
50 chanics a thin KL is a region of a strong discontinuity of
51 thermo- and gas-dynamics variables.^{6–10} The degree of non-

equilibrium (the intensity) of evaporation is conveniently
52 characterized by the Mach number on the outer boundary of
53 the KL. Upon irradiation with a constant intensity in vacuum
54 or in an environmental gas with a low counterpressure,
55 evaporation proceeds with a sonic velocity $M=1$,^{5,11} the ma-
56 terial flux through the phase boundary is the highest, the
57 process takes place under a strongest nonequilibrium, and the
58 behavior of the condensed medium is independent of the
59 state of the vapor region. Generally, subsonic evaporation
60 $M < 1$ is realized because of the counterpressure of the ex-
61 ternal gaseous medium^{12–14} or the previously vaporized
62 material,^{15,16} and the processes in the condensed and vapor
63 phases turn out to be interrelated.
64

Transition of a laser-irradiated matter from the con-
65 densed to the gaseous state can also proceed through other
66 mechanisms different from surface evaporation: volumetric
67 explosive boiling of the subsurface layer heated up to a near-
68 critical temperature^{17–19} or gas-dynamics outflow formed if
69 the temperature and (or) pressure at the surface exceed(s)
70 critical values.^{20,21}
71

The problem of back condensation to the irradiated
72 surface—the process opposite to surface evaporation—has
73 been the concern of a number of recent studies analyzing
74

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75 laser ablation.^{14,22–24} According to experimental data and
 76 analytical estimations,²² the amount of evaporated matter
 77 that condenses on the surface after the end of the nanosecond
 78 laser pulse ranges from 10% for a monatomic vapor to 43%
 79 for large molecules. Progress in numerical studies of the
 80 back condensation is based in a great extent on the results in
 81 Refs. 25 and 26, which formulated boundary conditions at
 82 the condensed medium-vapor interface and tabulated rel-
 83 evant calculation data.

84 The course of laser-induced evaporation changes quali-
 85 tatively if a plasma is formed in the evaporated matter. The
 86 most well-known consequence of the plasma formation is the
 87 absorption of incident laser radiation (screening effect) that
 88 affects the target heating and evaporation rate. The phenom-
 89 enon was analyzed numerically by one-dimensional^{23,27,28}
 90 (1D) and two-dimensional^{29–31} models. Properties of the
 91 laser-induced plasma are known to be dependent on the ra-
 92 diation wavelength.^{32–34} A comparative review of 1.06 and
 93 0.308–0.199 μm UV laser plasmas presented in Ref. 4
 94 shows that in the latter case the plasma appears to be colder
 95 and more transparent, allows for a greater removal of the
 96 target matter, and generates a moderate energy ion flux. With
 97 a nonuniform spatial distribution of the laser beam intensity
 98 the screening effect on the periphery of the plasma pattern
 99 can be weaker than in the center.³⁵

100 A much less studied effect of plasma formation is the
 101 generation of a high counterpressure, which was demon-
 102 strated to be as much important as the screening effect.^{36–38}
 103 high pressure of the plasma can not only decelerate but re-
 104 verse the direction of the phase transition and leads to the
 105 back condensation onto the surface during the laser pulse
 106 despite the target temperature being much higher than the
 107 equilibrium boiling temperature.

108 Plasma formation is normally accompanied by emission
 109 of thermal radiation that can transport energy out of the sys-
 110 tem or redistribute it. This phenomenon represents an impor-
 111 tant source of information on plasma parameters. Studies of
 112 the radiation transfer upon the laser action of microsecond
 113 and nanosecond durations were performed in Refs. 39–44. In
 114 particular, thermal radiation generated by the hot outer layer
 115 of the plasma pattern was shown to deliver energy to the
 116 surface of the target.^{39,41} According to Ref. 40 the radiative
 117 energy loss does not exceed 5%–10% of the total plasma
 118 energy for the microsecond action with the intensity of
 119 5–50 MW/cm^2 . For the nanosecond action, the increase of
 120 the radiation intensity from 10^9 to 2×10^{10} W/cm^2 aug-
 121 ments the radiative loss from 10% to 60%.⁴³

122 One more consequence of the plasma formation is a sig-
 123 nificant increase in gas-dynamics velocity in comparison
 124 with the nonionized vapor and the respective enhancement of
 125 lateral expansion. An example of the classification of plasma
 126 expansion regimes can be found in Ref. 45. Analysis of the
 127 transition from the one- to the three-dimensional (3D) expan-
 128 sion of ablation products upon the nanosecond action of
 129 neodymium-doped yttrium aluminum garnet (Nd-YAG) and
 130 ruby lasers with the intensity of 14 GW/cm^2 was performed
 131 in Ref. 46. The back condensation of evaporated matter out-
 132 side the irradiation spot caused by the lateral expansion was
 133 observed in Ref. 21. The widening of the energy distribution

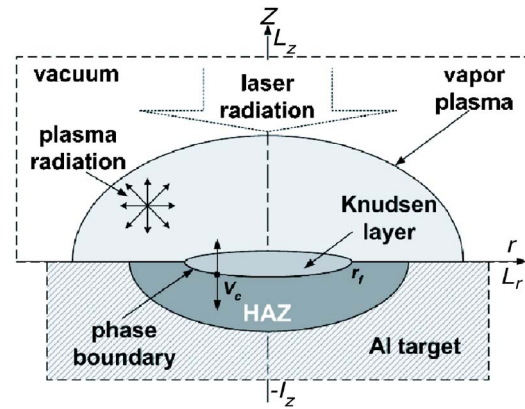


FIG. 1. (a) Setup and (b) reference frame of the problem.

zone at the surface due to the action of the thermal radiation
 of expanding plasma was pointed out in Ref. 47.

The main objective of the present study is a comparative
 analysis of the phase transition on the surface of an alumi-
 num target and of the properties of the vapor plasma induced
 by nanosecond laser radiation action at the wavelengths of
 1.06 μm in the IR range and 0.248 μm in the UV range with
 an intensity of 10^8 – 10^9 W/cm^2 in vacuum. The paper is
 organized as follows. Section II gives a brief presentation of
 the model. In Sec. III, the principal features of the phase
 transitions are considered, and the effects of plasma screen-
 ing, counterpressure, back condensation, and nonuniform in-
 tensity distribution are analyzed. Section IV is devoted to the
 structure of the plasma pattern, the effect of lateral expan-
 sion, and the role of thermal radiation. Qualitative compari-
 son of the predicted results with the available experimental
 data and analytic estimations is given in the course of the
 presentation. In Sec. V a more detailed comparison with data
 on threshold intensities of plasma formation and thickness of
 the removed layer is performed along with some consider-
 ations on the dependence of the found regularities on the
 target material and environment parameters.

II. PROBLEM STATEMENT

The physical model used^{37,38} accounts for the following
 phenomena: (i) surface heating of a metal target by laser
 radiation and conductive heat transfer; (ii) surface evapora-
 tion and back condensation; (iii) transfer and absorption of
 laser radiation in vapor plasma; (iv) gas-dynamics expan-
 sion, heating, and ionization of the plasma; and (v) genera-
 tion and transfer of thermal radiation, Fig. 1(a). The pro-
 cesses were mathematically described in a coordinate system
 comoving with the target surface. Its origin was located in
 the center of the laser beam, the r axis coincided with the
 surface, and the z axis was directed along the outward drawn
 normal, Fig. 1(b).

A. Condensed medium

In the region $0 < r < L_r$, $-l_z < z < 0$ occupied by a con-
 densed medium, Fig. 1(b), the heat transfer is described by
 the heat conduction equation:⁴⁸

173
$$\rho_c C_p \left(\frac{\partial T_c}{\partial t} + V_c \frac{\partial T_c}{\partial z} \right) = \frac{1}{r} \frac{\partial}{\partial r} \left(r K \frac{\partial T_c}{\partial r} \right) + \frac{\partial}{\partial z} \left(K \frac{\partial T_c}{\partial z} \right), \quad (1)$$

174 where the subscript c denotes the condensed medium, T_c is
 175 the temperature, V_c is the velocity of the evaporation (con-
 176 densation) front, and ρ_c , C_p , and K are the density, specific
 177 heat, and thermal conductivity. The absorption of the laser
 178 energy is described in the surface approximation; therefore
 179 the energy release term is not presented in Eq. (1) but in the
 180 interface boundary conditions (16) (see Sec. II C). The ap-
 181 proach is valid since the thermal wave penetration depth
 182 $[K/(\rho C_p) \times \tau]^{1/2} \sim 10^{-4}$ cm is much greater than the depth of
 183 the absorption layer $(\kappa_c)^{-1} \sim 10^{-6}$ cm, for the considered tar-
 184 get and laser pulse parameters.⁴⁹ Here τ denotes the laser
 185 pulse duration and κ_c is the absorption coefficient of the
 186 condensed medium.

187 The external boundaries of the region were assumed to
 188 be thermally insulated, the symmetry condition is fulfilled at
 189 $r=0$, and the initial target temperature is $T_0=300$ K. The
 190 target melting was excluded from consideration as it has a
 191 minor effect on the energy balance of the system because the
 192 latent melting heat is much smaller than the evaporation one.
 193 The model also does not account for hydrodynamic melt
 194 motion that insignificantly affects the surface phase transi-
 195 tions under nanosecond irradiation but would substantially
 196 complicate the model of the condensed medium and the
 197 computational algorithm.

198 **B. Gaseous medium and plasma**

199 The processes in the vapor region $0 < r < L_r$, $0 < z < L_z$,
 200 Fig. 1(b), were described by a system of radiative gas-
 201 dynamics equations and the laser radiation transfer
 202 equation:^{35,50}

203
$$\frac{\partial \rho}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u) + \frac{\partial}{\partial z} (\rho v) = 0, \quad (2)$$

204
$$\frac{\partial (\rho u)}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u^2) + \frac{\partial}{\partial z} (\rho u v) = - \frac{\partial P}{\partial r}, \quad (3)$$

205
$$\frac{\partial (\rho v)}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u v) + \frac{\partial}{\partial z} (\rho v^2) = - \frac{\partial P}{\partial z}, \quad (4)$$

206
$$\frac{\partial (\rho e)}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho u e) + \frac{\partial}{\partial z} (\rho v e)$$

 207
$$= - p \left[\frac{1}{r} \frac{\partial (r u)}{\partial r} + \frac{\partial u}{\partial z} \right] - \left(\frac{1}{r} \frac{\partial q_r}{\partial r} + \frac{\partial q_z}{\partial z} \right) + \left(\frac{\partial G}{\partial z} \right), \quad (5)$$

AQ: 208
$$\text{div } \mathbf{q}_v + c \kappa_\nu U_\nu = c \kappa_\nu U_{b\nu}, \quad \mathbf{q}_v = - \frac{c}{3 \kappa_\nu} \text{grad } U_\nu, \quad (6)$$

 #1 209

210
$$U_{b\nu} = \frac{8 \pi h \nu^3}{c^3 [\exp(h\nu/kT) - 1]},$$

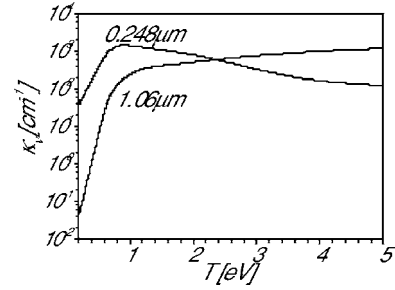


FIG. 2. Temperature dependency of plasma absorption coefficient $\kappa(T, \rho)$ at a fixed density $\rho=5 \times 10^{-3}$ g/cm³ for the laser wavelengths of 1.06 and 0.248 μm .

$$\frac{\partial G^-}{\partial z} - \kappa G^- = 0, \quad \frac{\partial G^+}{\partial z} + \kappa G^+ = 0, \quad G = G^- - G^+, \quad (7) \quad 211$$

$$0 < z < L_z, \quad 0 < r < 2r_f, \quad (7) \quad 212$$

$$P = P(\rho, T), \quad (8) \quad 214$$

$$e = e(\rho, T), \quad (9) \quad 215$$

$$\kappa_\nu = \kappa_\nu(\rho, T, \nu), \quad (10) \quad 216$$

where u and v are the components of the vapor velocity
 vector, ρ , P , and e are the density, pressure, and volume
 density of internal energy, $\mathbf{q} = \int \nu \mathbf{q}_\nu d\nu = (q_r, q_z)$ is the thermal
 radiation flux, κ_ν is the spectral absorption coefficient, U_ν
 and $U_{\nu,eq}$ are the volume density of plasma radiation and the
 blackbody radiation, and r_f is the laser beam radius. Equa-
 tions (2)–(4) describe the gas movement in Euler approxima-
 tion. The energy balance equation (5) accounts for the work
 of pressure, heating by the laser and thermal radiation, and
 neglects heat conduction. Equations (6) describe the radia-
 tion transfer in the diffusion approximation.^{50,51} The laser
 radiation transfer equation (7) takes into account both the
 component incident on the target G^- and the reflected one
 G^+ . The tabulated equations of the state [Eqs. (8) and (9)]
 were borrowed from Ref. 52. Absorption coefficients (10)
 were calculated by the approach of Ref. 53 based on the
 Hartree-Fock-Slater model. The equilibrium charge compo-
 sition of the plasma and the excited state distribution were
 determined by the Saha-Boltzmann equations.⁵¹

The absorption coefficient $\kappa = \kappa(T, \rho)$ of the laser radia-
 tion was determined in the same way as the coefficient κ_ν .⁵³
 Figure 2 shows two dependencies $\kappa(T, \rho=5 \times 10^{-3}$ g/cm³)
 related to the 1.06 and 0.248 μm radiations. For the 1.06 μm
 wavelength the inverse bremsstrahlung is the only absorption
 mechanism, and its contribution increases monotonically
 with temperature owing to the increase of the equilibrium
 concentration of electrons. For the 0.248 μm radiation the
 dependence is more complicated and includes the contribu-
 tion of both the inverse bremsstrahlung and the
 photoionization.^{23,51} The coefficient increases in the tempera-
 ture range $T < 1$ eV in which the photoionization of neutral
 atoms dominates. For higher temperatures $T > 1$ eV the co-
 efficient diminishes because nearly all neutrals are already
 ionized and the contribution of the photoionization decreases

251 rapidly. The comparison of the two curves shows that the
252 0.248 μm radiation heats plasma more effectively at low
253 temperatures, while at the temperature $T > 2$ eV absorption
254 of the 1.06 μm radiation becomes more intensive.

255 The model neglects scattering of photons caused mainly
256 by free electrons and characterized by a very small scattering
257 cross section of $\approx 7 \times 10^{-25}$ cm^2 (Refs. 42 and 51) (the so-
258 called Thomson cross section). For an electron density of
259 $\sim 10^{19}$ cm^{-3} typical for near-surface erosion plasma⁴ it cor-
260 responds to a scattering coefficient of $\sim 10^{-5}$ cm^{-1} and is
261 much smaller than the absorption coefficient, Fig. 2.

262 The system of equations (2)–(10) was supplemented
263 with the following initial and boundary conditions:

$$264 \quad t = t_0: \quad u = v = 0, \quad T = T_0, \quad \rho = \rho_0, \quad (11)$$

$$265 \quad 0 \leq (r \times z) \leq (L_r \times L_z),$$

$$267 \quad r = 0: \quad u = 0, \quad \partial \rho / \partial r = \partial v / \partial r = \partial P / \partial r = 0, \quad q_r = 0, \quad (12)$$

$$268 \quad r = L_r: \quad p = p_0, \quad \rho = \rho_0, \quad u = v = 0, \quad q_r = -cU/2, \quad (13)$$

$$269 \quad z = L_z: \quad p = p_0, \quad \rho = \rho_0, \quad u = v = 0, \quad q_z = -cU/2, \quad (14)$$

$$270 \quad G^- \equiv G_0 \exp[-(r/r_f)^2] \exp[-4(t/\tau - 1)^2], \quad 0 < r < 2r_f,$$

$$271 \quad z = 0: \quad z = 0: G^+ = [1 - A(T)]G^-, \quad 0 < r < 2r_f, \quad (15)$$

272 where τ is the laser pulse duration (full width at half maxi-
273 mum) and $A(T)$ is the surface absorptivity. Unlike for some
274 other metals (Cu, Au, Ag, and Pt) absorptivity of the pure
275 cold aluminum varies insignificantly in the spectral range of
276 interest and falls within the range of 5%–10%;^{4,54} therefore A
277 was assumed to be independent of the wavelength. The tem-
278 perature dependence was described by the expressions $A(T_c$
279 $< T_m) = 0.231$, $A(T_c > T_m) = 0.64T_c^{0.4}$ taken from Ref. 29. Ac-
280 cording to the second relationship, the surface absorbs ap-
281 proximately half of the incident radiation at $T_c = 6000$ K. The
282 effect of a significant increase of the surface absorptivity (by
283 three to five times) was also established in Refs. 4 and 55 for
284 the 0.308 μm laser radiation with the peak intensity of
285 10^9 W/cm^2 .

286 C. Interface boundary conditions

287 Boundary conditions at the interface relate six quantities:
288 the front velocity V_c , the temperature T_c and the pressure P_c
289 of the target surface with the temperature T , the density ρ ,
290 and the normal velocity v in the plasma at the external
291 boundary of the KL. The conditions are formulated in differ-
292 ent ways for the evaporation and condensation.²⁶ Independ-
293 ent of the direction of the phase transition the three conser-
294 vation laws are fulfilled:

$$\lambda_c \frac{\partial T_c}{\partial z} = AG^- + L_v \rho_c V_c, \quad \rho_c V_c = \rho(V_c - v), \quad (16) \quad 295$$

$$\rho_c V_c^2 + P_c = \rho(V_c - v)^2 + P, \quad (16) \quad 296$$

where L_v is the heat of evaporation. 298

In the case of evaporation, two additional relationships 299
of the Crout model were used:^{56,57} 300

$$\frac{T}{T_c} = \frac{2\gamma M^2(m^2 + 1/2)^2}{(1 + \gamma M^2)^2 m^2 t^2}, \quad (17) \quad 301$$

$$\frac{\rho}{\rho_{\text{sat}}} = \frac{tm^2(1 + \gamma M^2)[\gamma M^2(m^2 + 1/2)]^{-1}}{\exp(-m^2) + \pi^{1/2}m[1 + \text{erf}(m)]}, \quad (17) \quad 302$$

$$M = v/\sqrt{\gamma RT}, \quad \rho_{\text{sat}} = P_{\text{sat}}/(RT_c), \quad (17) \quad 303$$

$$P_{\text{sat}} = P_b \exp\left[\frac{L_v}{RT_c}\left(1 - \frac{T_b}{T_c}\right)\right], \quad (17) \quad 304$$

$$\left(1 + \frac{3\gamma M^2 - 1}{\gamma M^2 + 1}\right)(m^2 + 1/2)^2 - m^2(m^2 + \alpha + 3/2) = 0, \quad (18) \quad 305$$

$$\alpha = 2t^2 - 2^{-1}\pi^{1/2}mt - 1, \quad (18) \quad 306$$

$$t = \frac{2m}{\pi^{1/2}} + \frac{1 + \text{erf}(m)}{\exp(-m^2) + \pi^{1/2}m[1 + \text{erf}(m)]}, \quad (18) \quad 307$$

where ρ_{sat} and P_{sat} are the saturated vapor density and pres- 309
sure at the temperature T_c , R is the gas constant, γ is the 310
adiabatic exponent (equal to 5/3 for monatomic vapor), P_b 311
and T_b are the equilibrium pressure and temperature of boil- 312
ing under normal conditions, and m , t , and α are the auxil- 313
iary variables of the Crout model coupled by relationships 314
(18). The system of five relationships (16)–(18) has one free 315
parameter, the Mach number, that depends on gas-dynamics 316
flow conditions and was determined from Eqs. (2)–(5). It 317
was assumed that the velocity v of the evaporation flow does 318
not exceed the local sound velocity, $M \leq 1$.^{6–8,26,56} 319

On reaching the inequality $P_{\text{sat}} < P$ the phase transition 320
changes direction and evaporation is replaced by condensa- 321
tion $M < 0$ that may take place in both the subsonic and 322
supersonic regimes.²⁶ In the case of subsonic condensation 323
 $-1 < M < 0$, only one additional relationship was used:^{37,38} 324

$$P/P_{\text{sat}} = 0.95 \exp(2.42|M|) \quad (19) \quad 325$$

that approximates the tabular function $F_s(T/T_c, M) = P/P_{\text{sat}}$ 326
(Refs. 25 and 58) and neglects the rather weak dependence 327
of the F_s on the temperature ratio. For the supersonic regime 328
 $M < -1$, $P/P_{\text{sat}} > 10$ all the three fluid parameters at the KL 329
were determined from Eqs. (2)–(5).^{26,38} 330

D. Algorithm of numerical solution 331

The differential model (1)–(19) was solved by the finite 332
difference (FD) technique. The computational grid contained 333
50–100 nodes along the r axis in the region $0 < r < L_r$ 334
 $= 5$ cm and was denser in the region of the laser spot, Fig. 335
1(b). The nonuniform grid along the z axis was separately 336

337 constructed in the condensed ($L_z=0.01$ cm, 40 nodes) and
 338 gaseous ($L_z=10$ cm, 100–200 nodes) regions. In both regions
 339 the grid became denser toward the target surface; the first
 340 steps were equal to 2×10^{-6} and 10^{-5} cm, respectively. The
 341 heat conduction equation with a convective term and
 342 temperature-dependent coefficients was approximated by a
 343 fully implicit difference scheme written on a five-point pat-
 344 tern and was solved by the alternating direction method with
 345 iterations.⁵⁹ A detailed description of the FD method used for
 346 radiative gas-dynamics equations is given in Refs. 40, 49,
 347 and 60. The computational algorithm of the problem as a
 348 whole took into account the interrelation of the processes and
 349 included three stages at each time step: solution of the equa-
 350 tions in the gaseous state, calculation of relationships at the
 351 interface, and solution of the equation in the condensed me-
 352 dium. All the three stages were repeated in the outer loop.³⁶

353 III. PHASE TRANSITIONS ON THE TARGET 354 SURFACE

355 Let us turn now to the presentation and discussion of the
 356 results. In this section the regularities of the phase transition
 357 are considered induced by the 1.06 and 0.248 μm lasers with
 358 a fixed pulse duration $\tau=20$ ns. The influence of the radia-
 359 tion intensity and the beam radius is analyzed by varying
 360 $G_0 \in 10^8\text{--}10^9$ W/cm² and $r_f \in 0.005\text{--}0.25$ cm [Eq. (14)] in
 361 respect to their reference values of 5×10^8 W/cm² and
 362 0.025 cm. The intensity distribution is Gaussian in space that
 363 provides nonuniform irradiation conditions. The main ana-
 364 lyzed variables of the predicted solution are the intensity of
 365 the transmitted laser radiation G_s , the surface temperature T_c ,
 366 the plasma counterpressure P_{pl} , the Mach number M , and the
 367 removed layer thickness H_v .

368 Parameters of the aluminum used in calculations are
 369 $T_b=2720$ K, $P_b=1$ bar, $L_v=1.1 \times 10^4$ J/g, and A_m
 370 $=27$ g/mol.⁴⁹ Values of the thermal conductivity, heat capac-
 371 ity, and density were specified taking into account the differ-
 372 ence between the solid $T_c < T_m$ and liquid $T_c > T_m$ phases:
 373 $K=2.37$ and 0.75 W/(cm K), $C_p=0.95$ and 1.2 J/(g K), and
 374 $\rho_c=2.7$ and 2.33 g/cm³ (the melting temperature T_m
 375 $=933$ K).^{36,49}

376 The background density ρ_0 of 3×10^{-6} g/cm³ was taken
 377 as corresponding to the background pressure $p_0=2$
 378 $\times 10^{-3}$ bar.

379 A. Plasma transmission

380 The transmission coefficient is one of the most important
 381 optical characteristics of a plasma. It shows which part of the
 382 laser energy reaches the target and is spent for heating and
 383 removal of the material. Figure 3 represents time dependen-
 384 cies of this quantity $T_{\text{pl}}=G^-(r,z=0)/G^-(r,z=L_z)$ taken in the
 385 beam center $r=0$ and at the boundary $r=r_f$ for the 1.06 and
 386 0.248 μm radiations with $G_0=5 \times 10^8$ W/cm² and r_f
 387 $=0.025$ cm. The dashed lines in the figures indicate the ac-
 388 tion time and the shape of the laser pulse. For the 1.06 μm
 389 radiation the vapor remains transparent for some time after
 390 the onset of evaporation, Fig. 3(a). In the beam center, a
 391 sharp decrease of the transmission occurs at the instant t^*
 392 ≈ 17 ns with a minimum value of about 3% and corresponds

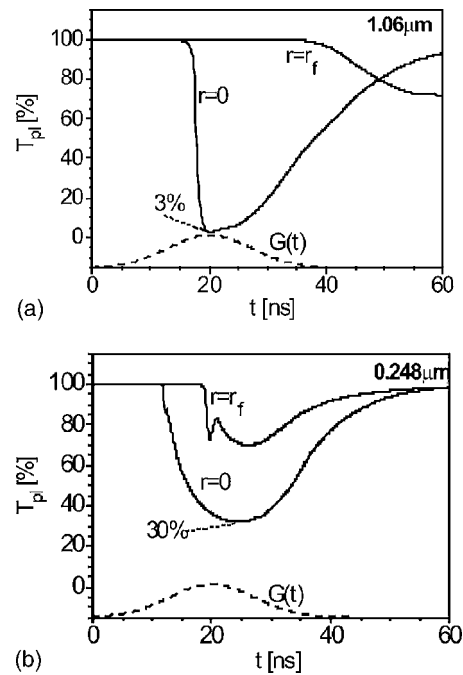


FIG. 3. Evolution of the plasma transmission $T_{\text{pl}}(t,r)=G^-(t,r,z=0)/G^-(t,r,z=L_z)$ in the beam center $r=0$ and at the boundary $r=r_f$ for the laser wavelengths of (a) 1.06 μm and (b) 0.248 μm , $G_0=5 \times 10^8$ W/cm², and $r_f=0.025$ cm. Dashed line indicates the action time and the shape of the laser pulse.

to the initiation of the plasma. On the other hand, at the beam 393
 boundary the coefficient remains equal to about 100% for the 394
 whole period of irradiation, thus indicating that there is no 395
 plasma above this region of the target. For the 0.248 μm 396
 radiation the picture is qualitatively different, Fig. 3(b), r 397
 $=0$: the decrease of the transmission begins just after the 398
 onset of evaporation at $t^* \approx 10$ ns but even at its minimum 399
 the coefficient does now fall below 30%. The dependence at 400
 $r=r_f$ is similar to the one in the center, but the plasma re- 401
 mains more transparent here and the minimum of transmis- 402
 sion is as high as about 70%. 403

The obtained results are in rather good agreement with 404
 the available data on plasma transparency δ , $T_{\text{pl}}=\exp(-\delta)$, 405
 measured for the similar action parameters $G_0=10^9$ W/cm² 406
 and $\tau=20\text{--}30$ ns: $\delta=2\text{--}3$ ($T_{\text{pl}} \approx 5\% \text{--}10\%$) for the 1.06 407
 μm (Ref. 17) wavelength and $\delta \approx 0.25$ ($T_{\text{pl}} \approx 75\%$) for the 408
 0.308 μm .^{4,55} A more detailed comparison of the numerical 409
 and experimental results would be complicated by the het- 410
 erogeneity of the plasma. 411

B. Action of the 1.06 μm laser radiation

Let us proceed with further considerations on the phase 413
 transition on the surface induced by the transmitted laser 414
 radiation. The time dependencies of the Mach number 415
 $M(t,r=0)$, the surface temperature $T_c(t,r=0)$, the saturated 416
 vapor pressure $P_{\text{sat}}(t,r=0)$ and the plasma pressure $P_{\text{pl}}(t,r$ 417
 $=0)$ in the beam center ($r=0,z=0$) for the laser pulse with 418
 $G_0=5 \times 10^8$ W/cm² and $r_f=0.025$ cm are plotted in Fig. 4. 419
 The surface temperature that grows monotonically for the 420
 leading edge of the laser pulse lowers sharply at the instant 421
 of plasma formation before reaching the critical value of 422

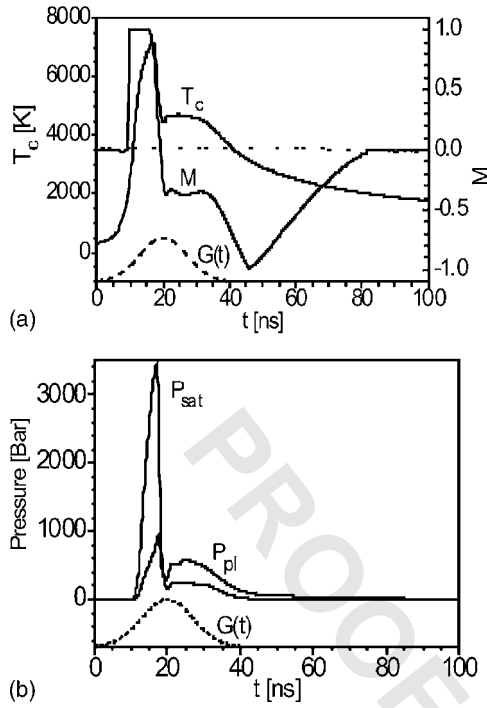


FIG. 4. Evolution of (a) the target surface temperature T_c and Mach number M . (b) Saturated vapor pressure P_{sat} and plasma pressure P_{pl} at the beam center $r=0$, $z=0$ for the laser wavelength of $1.06 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

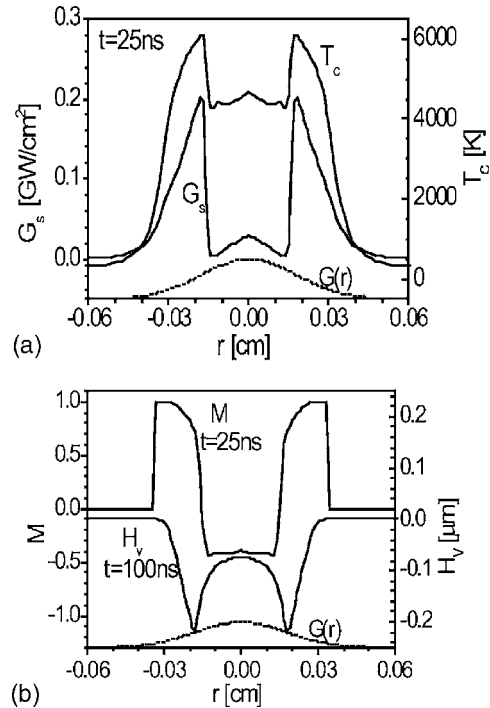


FIG. 5. Spatial distributions of (a) the transmitted intensity $G_s(t=25 \text{ ns}, r)$ and the surface temperature $T_c(t=25 \text{ ns}, r)$. (b) The Mach number $M(t=25 \text{ ns}, r)$ and the removed layer thickness $H_v(t=100 \text{ ns}, r)$ for the laser wavelength of $1.06 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

423 8000 K for aluminum,⁴⁹ Fig. 4(a). Simultaneously the Mach
 424 number starts to decrease from the $M=1$ level (the sonic
 425 velocity of the evaporated flux) to negative values $-1 < M$
 426 < 0 corresponding to the subsonic condensation. The vapor
 427 condensation is accompanied by the release of the heat of
 428 evaporation that compensates the conductive heat loss and,
 429 as a result, the temperature stabilizes at the level of approxi-
 430 mately 4500 K, which is much higher than the equilibrium
 431 boiling temperature. The two stages of the phase transition
 432 are also well seen in Fig. 4(b) that presents the dependencies
 433 of the saturated vapor pressure P_{sat} and the counterpressure
 434 of the plasma P_{pl} . For the preplasma stage, the saturated
 435 vapor pressure is several times higher and the necessary con-
 436 dition of evaporation is fulfilled $P_{sat} > P_{pl}$. After the plasma
 437 formation the counterpressure increases while P_{sat} drops
 438 down following the cooling of the surface, and on reaching
 439 the condition $P_{sat} < P_{pl}$ the vapor outflow becomes com-
 440 pletely suppressed and condensation begins.

441 The phase transition in the entire irradiated region is
 442 illustrated by the dependencies of the transmitted radiation
 443 intensities $G_s(t, r)$, the surface temperature $T_c(t, r)$, and the
 444 Mach number $M(t, r)$ at $t=25 \text{ ns}$ as well as the thickness of
 445 the removed layer $H_v(t, r)$ at the end of the computation t
 446 $= 100 \text{ ns}$, Fig. 5. The plots clearly show that the processes in
 447 the central and outer regions of the laser spot pass in differ-
 448 ent ways. In the central region $|r| < \approx r_f/2$ the plasma
 449 screens radiation that leads to a steplike drop of the G_s and
 450 T_c curves, Fig. 5(a). Note that the G_s value at the edge of the
 451 hollow corresponds to the threshold of the plasma formation
 452 for the $1.06 \mu\text{m}$ wavelength (see Sec. V A). Respectively, in
 453 the central region evaporation changes to condensation M
 454 < 0 , while in the outer region $|r| \approx r_f/2$ the intensive

evaporation with $M \approx 1$ persists, Fig. 5(b). The total effect of
 the phase transition is given by the removed layer thickness
 obtained by integrating the front velocity: $H_v(r, t) = \int_0^t V_c(r, t') dt'$,
 Fig. 5(b). As evident from this plot, the contribution of the
 central region to the total mass removal is much smaller than
 the one of the zone near the beam boundary. The $H_v(r)$ should
 not be identified with the final shape of an ablation crater
 because the latter is substantially affected by hydrodynamics
 of the melted near-surface layer. The characteristic time of
 this transformation is longer than $r_f/u_{s,l} \sim 100 \text{ ns}$, where
 $u_{s,l}$ is the sound velocity of the liquid aluminum.

The dependencies of the Mach number $M(t)$ in the beam
 center, Fig. 6, illustrate how the found regularities of the
 phase transition vary for the different radiation intensities
 $G_0=2 \times 10^8 - 10^9 \text{ W/cm}^2$ and beam radii $r_f=0.005 - 0.25$
 cm. As seen in Fig. 6(a), with higher intensity the Mach
 number becomes positive again after the period of condensation,
 $M < 0$; owing to the earlier formation of the plasma, it has
 time to partially restore its transparency before the end of the
 laser pulse and thus enables the evaporation to resume in the
 subsonic regime. The increase of the beam radius relative to
 the reference value of 0.025 cm has almost no effect on
 phase transition, Fig. 6(b), while for a smaller radius
 $r_f=0.005 \text{ cm}$ the difference is well noticeable: a small-
 volume amount of the evaporated matter expands very rapidly
 and the condensation after the laser pulse is not realized.

The $H_v(t)$ curves in Fig. 7(a) show evolution of the re-
 moved layer thickness with the different action parameters. The
 second rising interval of curves 1 (predicted for the smallest
 radius of 0.005 cm) and 2a (the highest intensity of

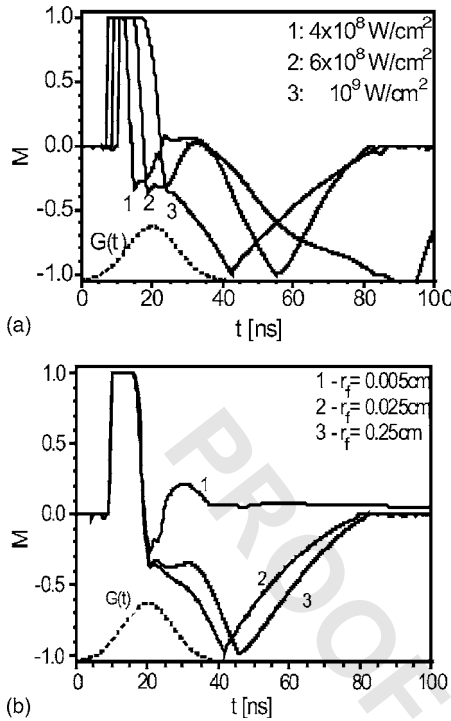


FIG. 6. Evolution of the Mach number $M(t, r=0)$ for (a) different peak intensities G_0 , $r_f=0.025$ cm and (b) different beam radii, $G_0=5 \times 10^8$ W/cm² for the laser wavelength of $1.06 \mu\text{m}$.

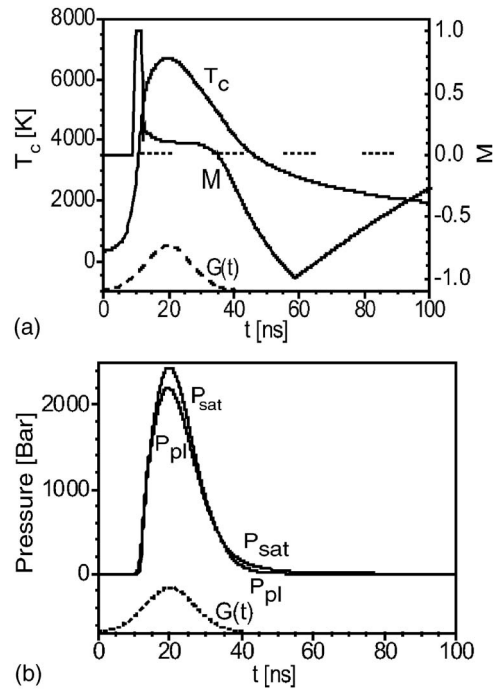


FIG. 8. Evolution of (a) the target surface temperature T_c and Mach number M . (b) Saturated vapor pressure P_{sat} and plasma pressure P_{pl} in the beam center $r=0$, $z=0$ for the laser wavelength of $0.248 \mu\text{m}$, $G_0=5 \times 10^8$ W/cm², and $r_f=0.025$ cm.

487 10^9 W/cm²) corresponds to the subsonic evaporation in the
 488 presence of the plasma and demonstrates that the mass re-
 489 moval can be substantial during this period. The falling in-
 490 tervals of all the four curves correspond to condensation and
 491 demonstrate that the amount of the evaporated matter con-
 492 densed back to the surface in the beam center varies from
 493 10% (curve 1) to nearly 50% (curves 2 and 3). The total
 494 fraction of the condensed matter obtained by integrating
 495 along the r coordinate was found to be smaller, 10%–20%.
 496 The portion condensed after the end of the pulse does not
 497 exceed several percent.

498 The final thickness of the removed layer for the different
 499 beam radii $H_v(r_f)$ is shown in Fig. 7(b), solid line. When

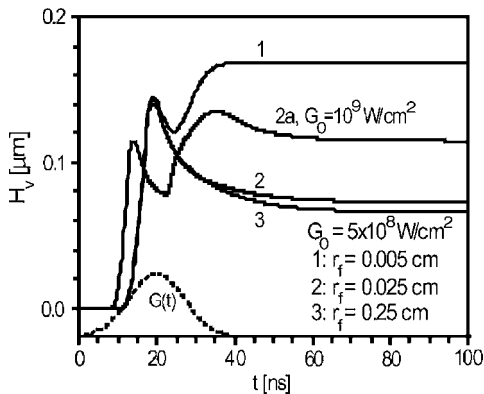


FIG. 7. (a) Evolution of the removed layer thickness at the beam center $H_v(t, r=0)$ for the different action parameters $G_0=5 \times 10^8$ W/cm², (1) $r_f=0.005$ cm, (2) $r_f=0.025$ cm, and (3) $r_f=0.25$ cm, and (2a) $G_0=10^9$ W/cm² and $r_f=0.025$ cm for the laser wavelength of $1.06 \mu\text{m}$: (b) Removed layer thickness vs beam radius $H_v(r_f)$ predicted with the account for the effect of plasma, solid line and neglecting plasma, dashed lines, $G_0=5 \times 10^8$ W/cm².

decreasing the radius the removed layer first varies insignifi- 500
 501 cantly and then, for the radii smaller than (~ 0.01 cm, begins
 502 to increase due to the lateral expansion of the plasma and
 503 reaches a value as high as $1-2 \mu\text{m}$. A similar effect of the
 504 increased evaporation efficiency for smaller beam radii was
 505 communicated in Ref. 17. The $H_v(r_f)$ dependence predicted
 506 by the model that does not account for the plasma formation
 507 is also shown, Fig. 7(b), dashed line. In this case the beam
 508 radius variation does not produce substantial variation of the
 509 thickness (a slight slope observed is due to the back condensa-
 510 tion): the expansion of the cold nonionized vapor proceeds
 511 with much lower velocity and has no time to manifest itself
 512 during the action even for the smallest beam radius consid-
 513 ered.

C. Action of the $0.248 \mu\text{m}$ laser radiation 514

Let us now analyze the phase transition induced by the 515
 0.248 μm UV laser radiation, Figs. 8–10. The instant of the 516
 plasma formation $t^* = 10$ ns is practically unnoticeable in the 517
 temperature plot but is well seen in the $M(t)$ dependence, 518
 Fig. 8(a). The stage of the sonic evaporation, $M=1$, turns out 519
 to be very short because of the early plasma formation. The 520
 most important difference as compared to the $1.06 \mu\text{m}$ ac- 521
 tion is that the evaporation does not stop after the plasma 522
 formation but continues in a subsonic regime $M \approx 0.1$ and 523
 condensation begins only after the end of the laser pulse. The 524
 corresponding pressure curves are shown in Fig. 8(b): the 525
 difference between the saturated vapor and plasma pressures 526
 $P_{\text{sat}} - P_{\text{pl}}$ substantially decreases but remains positive after 527
 the plasma formation. Note also that the maximum plasma 528
 pressure is much higher for the $0.248 \mu\text{m}$ radiation, P_{pl} 529
 ≈ 2000 bars, in comparison with the one for the $1.06 \mu\text{m}$ radia- 530

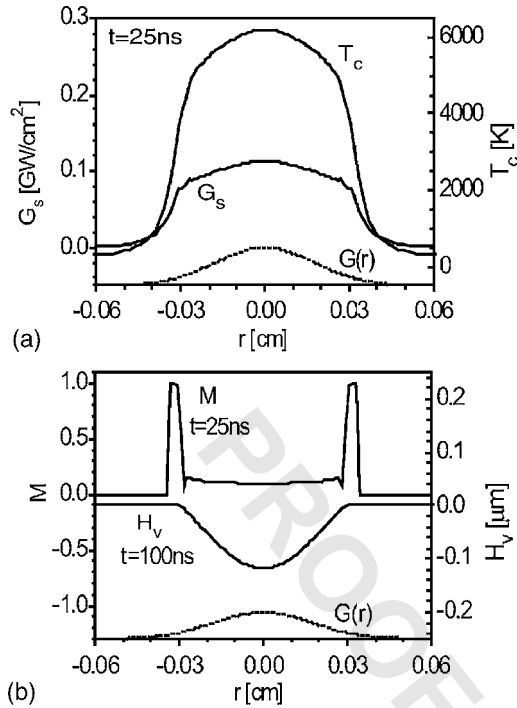


FIG. 9. Spatial distributions of (a) the transmitted intensity $G_s(t=25 \text{ ns}, r)$ and surface temperature $T_c(t=25 \text{ ns}, r)$. (b) The Mach number $M(t=25 \text{ ns}, r)$ and removed layer thickness $H_v(t=100 \text{ ns}, r)$ for the laser wavelength of $0.248 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

shape as compared to the one of the incident pulse, Fig. 9(a). The phenomenon is explained by a higher transmission of the plasma in the outer region of the spot that partially compensates the lower intensity of the incident pulse. The subsonic evaporation proceeds at approximately the same rate $M \approx 0.1-0.15$ throughout the spot region $|r| < r_f$, and the intensive evaporation with $M=1$ is observed only in the outermost part of the irradiation zone, Fig. 9(b). The final distribution of the removed layer thickness H_v has the shape of a hollow with smooth edges. The performed calculations showed that the intensity variation in the range of 10^8-10^9 W/cm^2 for the $0.248 \mu\text{m}$ laser radiation does not change qualitatively the course of the phase transition but only shifts the onset of evaporation, the plasma formation, and the transition to the subsonic regime to an earlier instant in time.³⁸

It is well seen from the removed layer thickness H_v curves in the beam center obtained for different action parameters, Fig. 10, that this quantity monotonically increases until the end of the laser pulse owing to the unceasing evaporation and only then yields place to the condensation. The total fraction of the condensed material decreases with decreasing the beam radius from 10% for $r_f=0.25 \text{ cm}$ to 4% for $r_f=0.025 \text{ cm}$ while for the radii smaller than $\sim 0.01 \text{ cm}$ the condensation is not realized. Note that the value of 10% corresponding to the greatest radius coincides with the result of Ref. 22 for condensation of the monatomic vapor produced by the nanosecond UV laser action with the fluency of 2 J/cm^2 in air.

On the whole, the presented results show that the surface phase transitions induced by the 1.06 and $0.248 \mu\text{m}$ radiations have a number of differences. In the former case the screening and retarding effect of the plasma is strong in the central part of the beam that stops evaporation and provokes a partial recondensation of the evaporated substance and is practically unnoticeable near the beam boundaries. In the latter case the plasma effect is weaker, it slows down evaporation but does not suppress it completely, and manifests itself over the entire surface of the irradiation spot.

IV. PLASMA CHARACTERIZATION

This section considers characteristics of the vapor plasmas induced by the 1.06 and $0.248 \mu\text{m}$ laser radiations. In Sec. IV A the temperature distribution $T(r, z)$ and the shape of the plasma pattern are compared for the effect of $G_0=5 \times 10^8 \text{ W/cm}^2$. In Sec. IV B the features of the pattern expansion are given as predicted for the different beam radii and, finally, in Sec. IV C the role of the plasma thermal radiation is analyzed by means of comparison of the plasma q_2 and laser G^- radiation fluxes.

A. Plasma temperature and pattern structure

Two-dimensional distributions of the plasma temperature at the instant of 25 ns for the action parameters $G_0=5 \times 10^8 \text{ W/cm}^2$, $r_f=0.025 \text{ cm}$, and the two wavelengths of 1.06 and $0.248 \mu\text{m}$ are shown in Figs. 11(a) and 11(b). At these parameters the plasma temperature is approximately the same—about $3-4 \text{ eV}$ —for both wavelengths, but the lo-

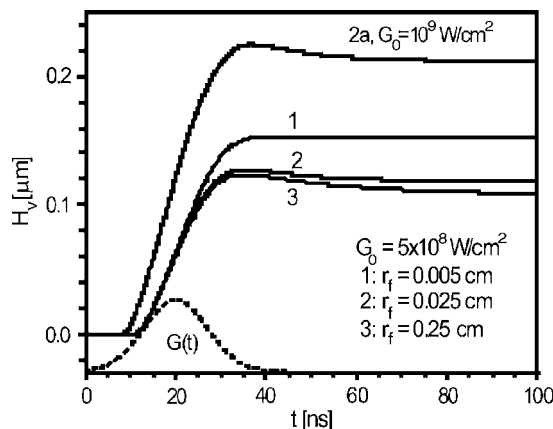


FIG. 10. Evolution of the removed layer thickness at the beam center $H_v(t, r=0)$ for the different action parameters $G_0=5 \times 10^8 \text{ W/cm}^2$, (1) $r_f=0.005 \text{ cm}$, (2) $r_f=0.025 \text{ cm}$, and (3) $r_f=0.25 \text{ cm}$, and (2a) $G_0=10^9 \text{ W/cm}^2$ and $r_f=0.025 \text{ cm}$ for the laser wavelength of $0.248 \mu\text{m}$.

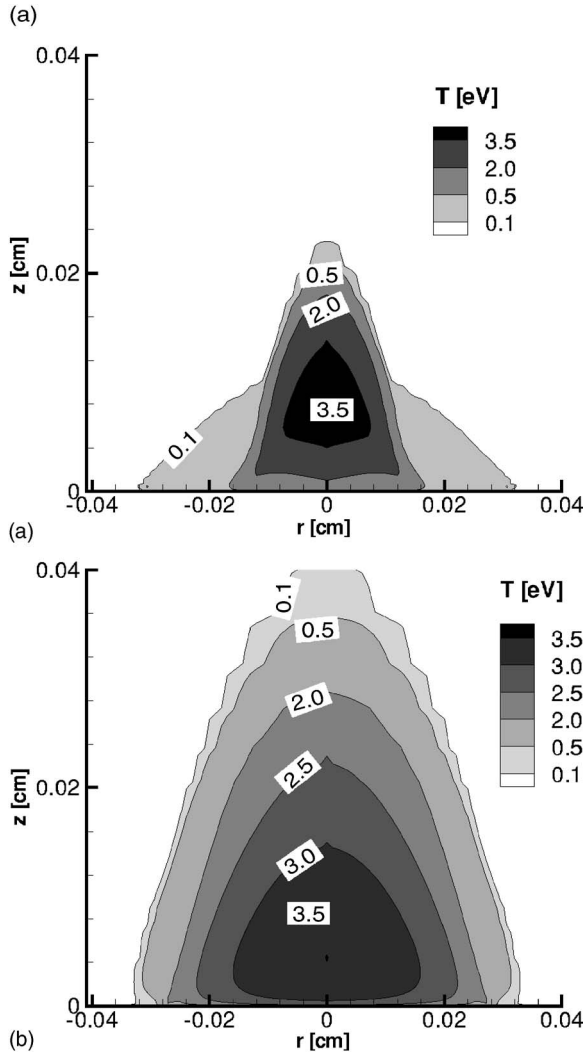


FIG. 11. Contour plot of the plasma temperature distribution $T(t=25 \text{ ns}, r, z)$ for the laser wavelengths of (a) $1.06 \mu\text{m}$ and (b) $0.248 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

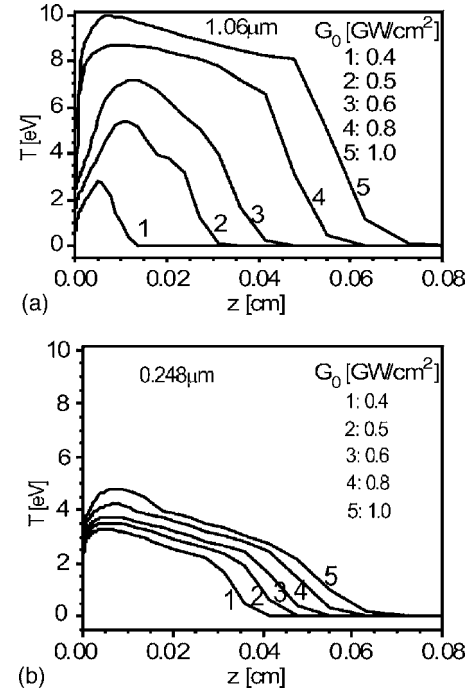


FIG. 12. Temperature distribution on the beam axis $T(t=25 \text{ ns}, r=0, z=0)$ for different intensities G_0 and the laser wavelengths of (a) $1.06 \mu\text{m}$ and (b) $0.248 \mu\text{m}$ and $r_f=0.025 \text{ cm}$.

for the action of 10^9 W/cm^2 . For the $0.248 \mu\text{m}$ radiation the efficiency of the laser heating drops down as soon as the temperature of 2–3 eV is reached because of the weakening of photoionization and the low efficiency of the inverse bremsstrahlung effect for the short wavelength radiation. As a result, the increase in radiation intensity does not lead to further plasma heating.

The observed distinction between the typical plasma temperatures for the IR and UV laser radiations is consistent with the data on plasma temperature cited in Ref. 4. In particular, the plasma of 10 eV was observed for the nanosecond action of $1.06 \mu\text{m}$ laser¹⁷ while the measured temperature did not exceed 2–3 eV for the $0.308 \mu\text{m}$ irradiation of approximately the same duration and intensity.^{55,61} The decrease in steady-state plasma temperature with the increasing energy of laser quantum for the microsecond pulses was discussed in Ref. 33.

B. Expansion of the plasma pattern

The plasma expansion for the $1.06 \mu\text{m}$ radiation is illustrated in Fig. 13, showing distributions of the plasma pressure (contour plots) and the gas-dynamics velocity (vector plots) for the different beam radii at two instants of time: $t=30 \text{ ns}$ (the final stage of the laser pulse) $r_f=0.25 \text{ cm}$ (a), $r_f=0.025 \text{ cm}$ (b), and $r_f=0.005 \text{ cm}$ (c) and $t=60 \text{ ns}$ (the stage of inertial expansion) $r_f=0.25 \text{ cm}$ (d), $r_f=0.025 \text{ cm}$ (e), and $r_f=0.005 \text{ cm}$ (f). For interpretation of the results a nondimensional time variable is introduced: $t'=(t-t^*)/t_{\text{gd}}$, $t_{\text{gd}}=r_f/u_{s,\text{pl}}$, where $u_{s,\text{pl}}$ is the sound velocity of the plasma.^{45,46} The $t' \ll 1$ and $t' \gg 1$ cases correspond to the one- and three-dimensional expansions, respectively, while the $t' \approx 1$ relates to the intermediate regime. The results in

600 cation of the hottest region, the “core,” is different: it is
 601 shifted toward the forefront of the pattern for the $1.06 \mu\text{m}$
 602 radiation and is adjacent to the target surface for the UV
 603 action. It was established that the position of the core coin-
 604 cides with the region where the incident laser radiation is
 605 released [see Fig. 15, $G^-(z)$ plot]. The size of the plasma
 606 pattern conditionally bounded by the isotherm $T=0.5 \text{ eV}$ is
 607 greater in both directions for the $0.248 \mu\text{m}$ radiation. For the
 608 z direction it is explained by the earlier instant of the plasma
 609 formation, and for the r direction by the wider region of the
 610 plasma initiation. Additionally, the “wings” of the pattern are
 611 well seen for the $1.06 \mu\text{m}$ radiation, Fig. 11(a), bounded by
 612 the isotherm of 0.1 eV . The wings consist of the nonionized
 613 vapor produced by the evaporation from the outer region of
 614 the irradiation spot, have the temperature of $0.1\text{--}0.3 \text{ eV}$, and
 615 are characterized by a much lower velocity of the gas-
 616 dynamics expansion than the one of the plasma core.
 617 The distributions of the plasma temperature at the beam
 618 axis $z=0$ for different radiation intensities are shown in Fig.
 619 12. The $1.06 \mu\text{m}$ radiation leads to a substantial plasma heat-
 620 ing with the maximum temperature as high as 10 eV reached

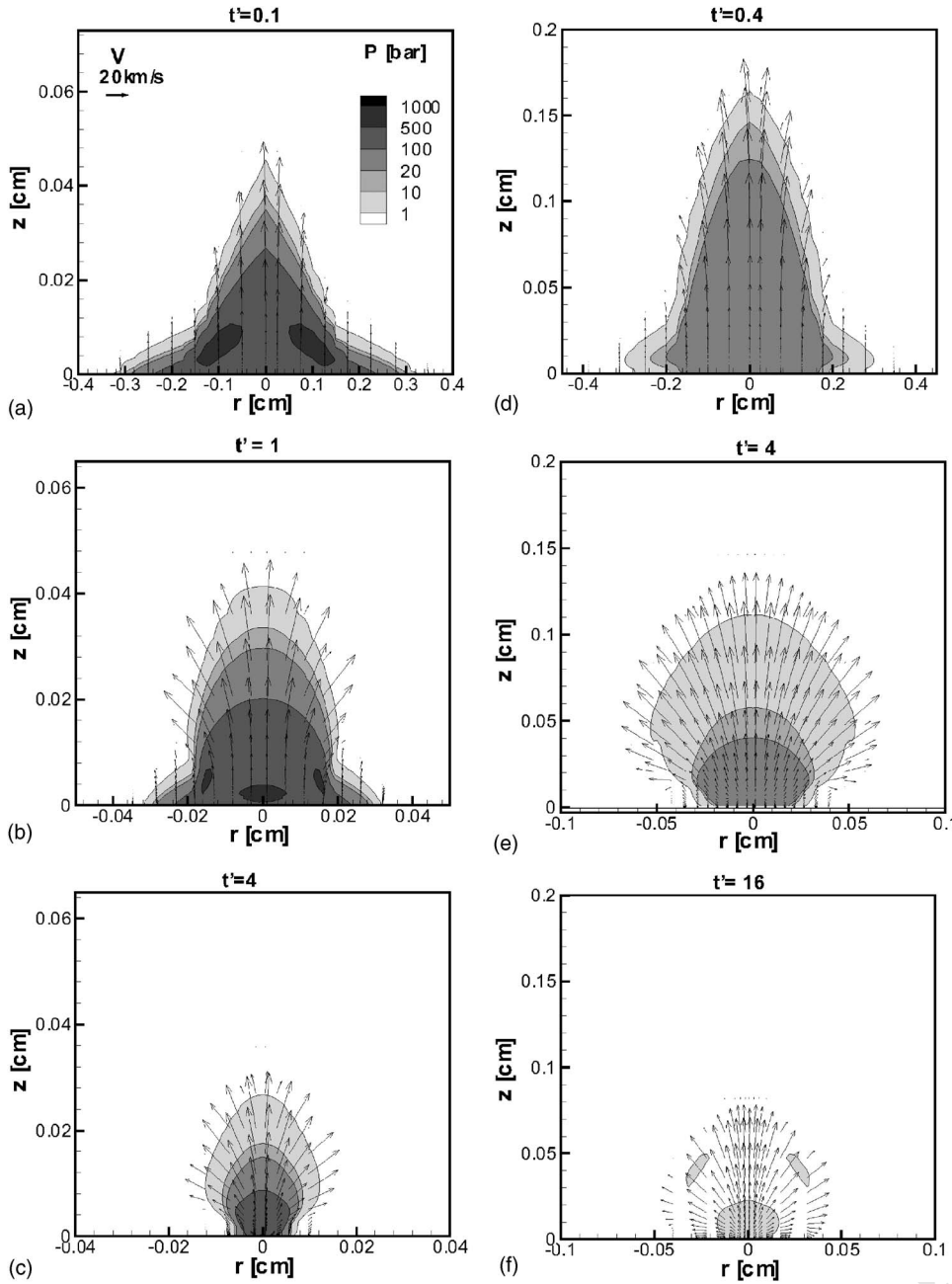


FIG. 13. Distributions of the pressure $P(t, r, z)$ (contour plot) and velocity vector $V(t, r, z)$ at the instants of $t = 30$ ns (a) $r_f = 0.25$ cm, (b) $r_f = 0.025$ cm, and (c) $r_f = 0.005$ cm and $t = 60$ ns, (d) $r_f = 0.25$ cm, (e) $r_f = 0.025$ cm, and (f) $r_f = 0.005$ cm, for the laser wavelength of $1.06 \mu\text{m}$ and peak intensity $G_0 = 5 \times 10^8 \text{ W/cm}^2$. Nondimensional time variable is defined as $t' = (t - t^*)/t_{\text{gd}}$, $t_{\text{gd}} = r_f/u_{s,\text{pl}}$, where t^* is the instant of plasma formation and $u_{s,\text{pl}}$ is the sound velocity of the plasma.

652 Figs. 13(a) and 13(d), predicted for the greatest beam radius
 653 correspond to the 1D expansion at both instants, $t' = 0.1$ and
 654 0.4. The expansion of the central part of the plasma in the z
 655 direction proceeds faster than the expansion of the colder
 656 wings leading to the formation of a “spacecraftlike” pattern.
 657 For the reference radius of 0.025 cm, Figs. 13(b) and 13(e), a
 658 noticeable lateral expansion begins at the end of the action,
 659 $t' = 1$, and becomes clearly 3D after the end of the pulse, t'
 660 $= 4$. The central part of the pattern expands mainly away
 661 from the target surface and in the lateral direction around the
 662 wings. Such an expansion explains, in particular, why the
 663 condensation is negligible after the laser pulse. For the
 664 smallest radius, Figs. 13(c) and 13(e), the expansion is three
 665 dimensional at both instants $t' = 4$ and $t' = 16$ that manifests
 666 itself in the weaker screening and the retarding effect of the
 667 plasma.

668 For the $0.248 \mu\text{m}$ radiation, the regularities of the
 669 plasma expansion are in general similar to the ones presented

above, Fig. 14, but the pattern structure is somewhat simpler 670
 owing to a more uniform vapor flow from the surface. The 671
 distinction of this regime is that the central part of the pattern 672
 expands both away and toward the surface, Fig. 14(b), lead- 673
 ing to a rather intensive condensation after the end of the 674
 pulse.³⁸ 675

C. Plasma thermal radiation 676

As it was shown in the studies dealing with the micro- 677
 second laser action, thermal radiation of plasma occasionally 678
 turns out to be the main mechanism of energy delivery to the 679
 target surface.^{27,36,41} Let us consider if this phenomenon 680
 takes place upon irradiation by nanosecond pulses. 681

The dependences of the thermal radiation flux $q_z(z)$, the 682
 incident laser radiation $G^-(z)$, the temperature $T(z)$, and the 683
 density $\rho(z)$ along the beam axis $r=0$ at the instant t 684
 $= 25$ ns are plotted in Fig. 15 for the $1.06 \mu\text{m}$ (a) and 685

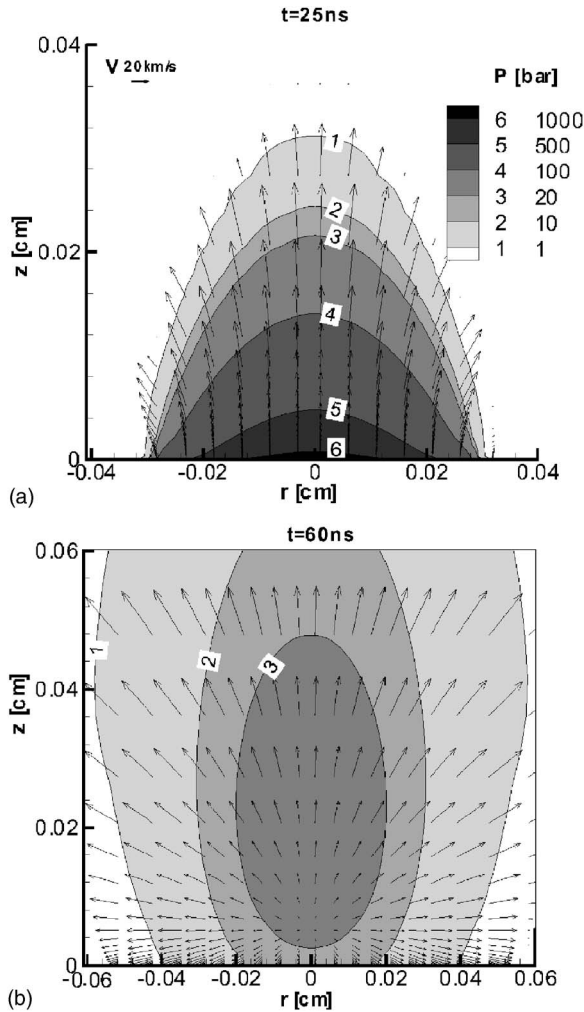


FIG. 14. Distributions of the pressure $P(t, r, z)$ (contour plot) and velocity vector $V(t, r, z)$ at the instants of (a) 25 ns and (b) 60 ns for the laser wavelength of $0.248 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

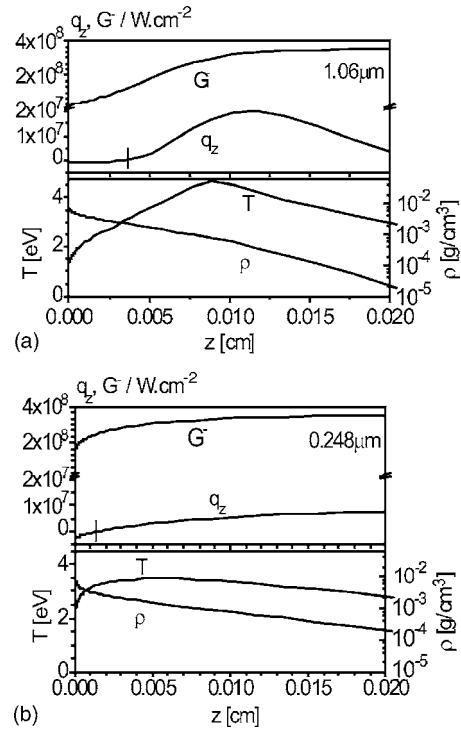


FIG. 15. Distributions of laser intensity G^- , z component of the thermal radiation flux q_z , plasma temperature T , and density ρ on the beam axis $r=0$ at the instant $t=25 \text{ ns}$, for the laser wavelengths of (a) $1.06 \mu\text{m}$ and (b) $0.248 \mu\text{m}$, $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$. Small vertical lines mark the right boundary of the zone where q_z is negative and plasma emits radiation towards the target.

The proportion of the laser and thermal radiation fluxes is illustrated by its dependencies on r coordinate, $t=25 \text{ ns}$. For the $1.06 \mu\text{m}$ radiation the radial size of the plasma pattern is about $r_f/2$ and the thermal radiation flux is nonzero in this region only. For the $0.248 \mu\text{m}$ radiation q_z is greater and has a wider distribution, but in both cases the laser flux exceeds the thermal radiation flux over the entire irradiation zone. It was also established that after the end of the laser pulse the thermal radiation flux decreases rapidly and does not produce a significant effect.

Plasma emissivity is the quantity that characterizes the emission of the homogeneous plasma layer of thickness L , temperature T , and density ρ , $\varepsilon=\varepsilon(L, T, \rho)$: $q=\varepsilon\sigma T^4$. The numerical values of these characteristics $\varepsilon=q_{z,\text{max}}/\sigma T_{\text{max}}^4$

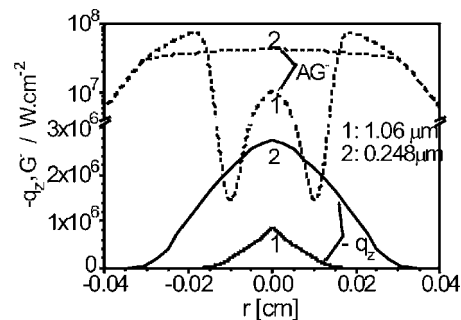


FIG. 16. Distributions at the target surface of the absorbed intensity of laser radiation $AG^-(t=25 \text{ ns}, r, z=0)$ and the intensity of thermal radiation $-q_z(t=25 \text{ ns}, r, z=0)$ for the laser wavelengths of $1.06 \mu\text{m}$ (curves 1) and $0.248 \mu\text{m}$ (curves 2), $G_0=5 \times 10^8 \text{ W/cm}^2$, and $r_f=0.025 \text{ cm}$.

$0.248 \mu\text{m}$ (b) radiations with $G_0=5 \times 10^8 \text{ W/cm}^2$ and $r_f=0.025 \text{ cm}$. For the $1.06 \mu\text{m}$ irradiation the maximum of the radiation flux is reached in the highest temperature region and is directed away from the target, $q_z > 0$, Fig. 15(a). The flux toward the target $q_z < 0$ is much weaker and attenuates further in the colder near-surface layer. The described picture of the radiation field is similar to the two-layer model of a plasma proposed in Ref. 41. The principal distinction, however, consists in that the laser radiation flux exceeds the flux of the thermal radiation by approximately an order of magnitude. The weakness of the plasma radiation is due to its relatively low temperature and the small effective thickness of the emitting layer which is of the order of the beam radius $\sim r_f$ (see also the analysis of Fig. 17).

The distinction of the thermal radiation field for the $0.248 \mu\text{m}$ radiation is related to a different structure of the plasma pattern: the flux toward the target is formed just near the surface and turns out to be much higher than the one for the $1.06 \mu\text{m}$ radiation, Fig. 15(b). However, the attenuation of the laser flux is also much weaker in this case, therefore the contribution of the plasma radiation to the total energy flux at the surface remains negligible.

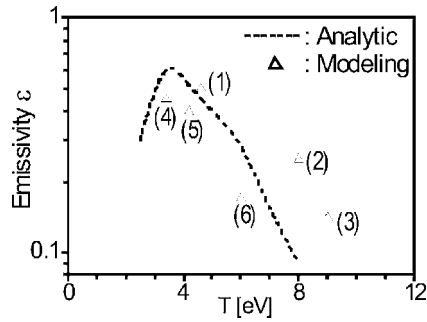


FIG. 17. Analytic emissivity of plasma layer taken from Ref. 41, Fig. 10(b), $L=0.03$ cm, $\rho=1.2 \times 10^{-3}$ g/cm³, dashed line and calculated values of emissivity $\varepsilon=q_{z,\max}/\sigma T_{\max}^4$ (averaged over the period of time 20–30 ns) for the laser wavelength of 1.06 μm , (1) $G_0=5 \times 10^8$ W/cm², (2) 8×10^8 W/cm², (3) 10^9 W/cm², and 0.248 μm , (4) $G_0=5 \times 10^8$ W/cm², (5) 8×10^8 W/cm², and (6) 10^9 W/cm², $r_f=0.025$ cm.

TABLE I. Comparison of the experimentally measured threshold intensities for the vapor plasma formation with the numerically predicted values.

Wavelength (μm)	1.06	0.532	0.355	0.308	0.248		
Reference	62	63	63	55	61	64	65
Pulse duration (ns)	7	6	6	20	20	15	17
Threshold intensity (experiment) (10^8 W/cm ²)	14	3.8	3.0	2.0	2.2	1.15	1.85
Threshold intensity (modeling) (10^8 W/cm ²)	10	4.3	2.9	1.1	1.1	1.2	1.25

Table I, rows 1–4. Row 5 presents the threshold intensities predicted numerically for the same action parameters by using the condition of the electron-ion collision domination over the electron-neutral ones $\nu_{ei} > \nu_{en}$ as the criteria of the plasma formation.^{4,66} The numerical results underestimate the experimental values in most of the cases, but the trend of the two dependencies is the same: the threshold intensity lowers down with the wavelength decreasing.^{32,33,66} A more detailed comparison is not expedient first of all because of the different criteria of the plasma formation. The inaccuracy of the model is also explained by the application of the equilibrium description for the plasma formation phenomenon (optical breakdown). A more correct determination of the threshold intensities is possible by means of a kinetic model of nonequilibrium plasma^{32,66} coupled with the expansion gas dynamics.

The spectral dependence of the threshold intensity $G^*(\lambda)$ predicted for the fixed duration of the laser pulse $\tau=20$ ns is presented in Table II. The intensity begins to decrease approximately at the boundary of the visible spectrum. In particular, the threshold value for the 1.06 μm Nd:YAG laser is approximately three times higher than the one for the lasers of the UV range.

B. Removed layer thickness

The mean thickness of the removed layer is likely the most often analyzed quantity in the experimental and numerical studies of the laser ablation. In this subsection experimental results on the nanosecond laser ablation of aluminum in vacuum at different wavelengths are used.^{17,55,65,67} In the modeling the following four parameters of the laser effect were taken approximately the same as in the experiments: laser wavelength, peak intensity, pulse duration, and beam radius.

Lasers of 1.06 and 0.532 μm . An experimental study of evaporation in vacuum for a number of materials induced by the 1.06 μm laser with the peak intensity of 10^8 – 5×10^9 W/cm², the pulse duration of 30 ns, and the beam radius of 20–250 μm was performed in Ref. 17. It was established that for the group of metals (Ti, Al, and W) and the

(averaged over the period of 20–30 ns) are shown in Fig. 17 by triangles for the 1.06 μm radiation, $G_0=(5, 8, \text{ and } 10) \times 10^8$ W/cm², points (1), (2), and (3) and the 0.248 μm , $G_0=(5, 8, \text{ and } 10) \times 10^8$ W/cm², points (4), (5), and (6). The analytic dependence (dotted line) is taken from Ref. 41 [Fig. 10(b)] for the parameters $L=0.03$ cm and $\rho=1.2 \times 10^{-3}$ g/cm³ which are representative for the plasma pattern shown in Fig. 15, plots T and ρ . The numerical analytic values are in reasonable agreement, in particular, the tendency of the emissivity to decrease with increasing temperature is clearly seen. As it was established by modeling, the total radiative energy loss is 3%–6% of the accumulated plasma energy during the laser pulse and approximately as much at the stage of the inertial expansion and cooling.

V. COMPARISON WITH EXPERIMENT AND DISCUSSION

In the previous sections some experimental results were already mentioned which were found to be qualitatively consistent with the numerical predictions. In this section a more accurate comparison is performed dealing with the threshold laser intensity of the plasma formation (Sec. V A) and the thickness of the removed layer (Sec. V B). Also some considerations are given as to how the found regularities depend on the target material and environment parameters (Sec. V C).

A. Threshold intensities of plasma formation

Threshold intensity of the nanosecond laser irradiation of an aluminum target in vacuum leading to the plasma formation was measured in Refs. 55 and 61–65. The plasma initiation was identified by means of either the pattern emission or a sharp increase of the ion flux. The used action parameters and the found threshold values are presented in

TABLE II. The predicted values of the threshold intensities for the vapor plasma formation for the different values of laser wavelength and the fixed pulse duration of 20 ns.

Laser	Nd:YAG	Ga-As	Ruby	HeNe	Nd:YAG	XeF	XeCl	KrF	ArF
Wavelength (μm)	1.06	0.9	0.694	0.639	0.532	0.351	0.308	0.248	0.193
Threshold intensity G^* (10^8 W/cm)	2.6	2.6	2.5	2.4	2.15	1.65	1	1.05	1

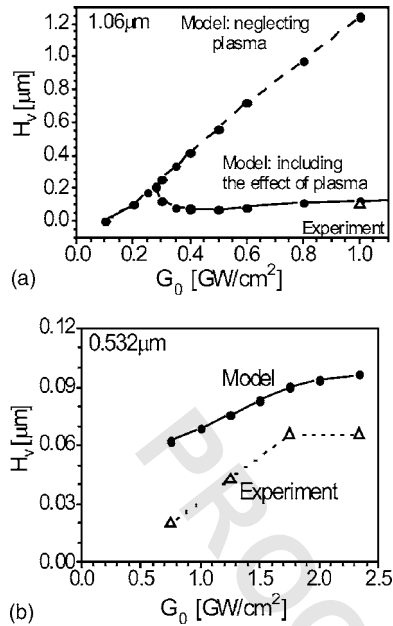


FIG. 18. Removed layer thickness vs laser intensity $H_v(G_0)$ predicted numerically with the account for the effect of plasma (solid lines), neglecting plasma (dashed lines), or found experimentally (triangles) (Refs. 17, 46, and 67) for the laser wavelengths of (a) 1.06 μm and (b) 0.532 μm and $r_f = 0.025$ cm.

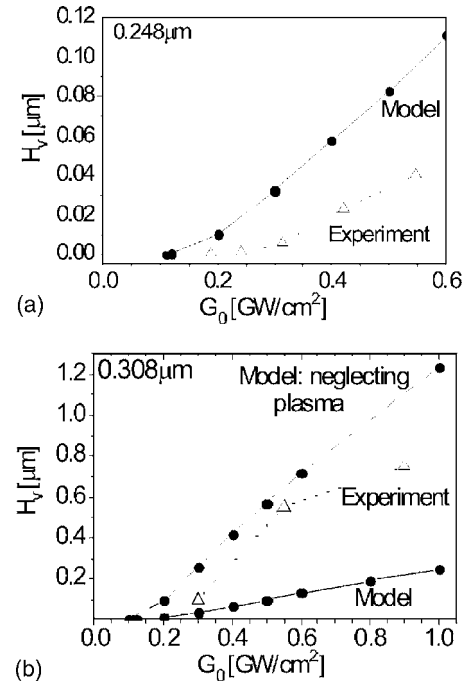


FIG. 19. Removed layer thickness vs laser intensity $H_v(G_0)$ predicted numerically and found experimentally for the laser wavelengths of (a) 0.248 μm (Ref. 65) and (b) 0.308 μm (Ref. 55).

793 laser intensity greater than 5×10^8 W/cm² the thickness of
 794 the removed layer was approximately constant and lied in the
 795 range of 0.05–0.1 μm. The particular value for Al (Refs. 17
 796 and 46) for the intensity of 10^9 W/cm² was about 0.1 μm,
 797 Fig. 18(a), triangle. The solid curve in the same figure shows
 798 the numerical dependence of the removed layer predicted by
 799 the model: the thickness increases for the subthreshold inten-
 800 sities, sharply decreases, passes through minimum, and then
 801 demonstrates a slow increase with a much lower slope in
 802 comparison with the preplasma regime. The particular result
 803 for the intensity of 10^9 W/cm² is somewhat greater than the
 804 experimental value. The same figure shows the dependence
 805 $H_v(G_0)$ predicted without account for the plasma effect, Fig.
 806 18(a), dashed line: the thickness increases monotonically and
 807 with constant rate over the entire range of intensities, exceed-
 808 ing the experimental value by more than an order of magni-
 809 tude.

810 Experimental data for the 0.532 μm Nd:YAG laser of
 811 the visible range with the peak intensity of (0.7–2.4)
 812 $\times 10^9$ W/cm², the pulse duration of 6 ns, and the beam ra-
 813 dius of 0.06 cm are marked by triangles in Fig. 18(b).⁶⁷ The
 814 removed layer thickness first increases and then approaches
 815 the constant level of about 0.06 μm. The numerical depen-
 816 dence, solid line, demonstrates a similar behavior but gives
 817 values overestimated by a factor of 1.5–3.

818 *Lasers 0.248 and 0.308 μm.* While analyzing the thick-
 819 ness of the layer removed by UV laser radiation, an addi-
 820 tional complexity arises from the injection of macroparticles
 821 from the target surface.^{4,68} The contribution of this mecha-
 822 nism to the total mass removal can be substantially reduced
 823 if the target is rotated between the subsequent laser pulses
 824 and thus the irradiated spot is shifted partially or completely
 825 to a virgin part of the surface. It was pointed out in Refs. 65

and 68 that by applying the target rotation technique the
 removed mass occasionally decreased by a factor of 5–10.

Triangles in Fig. 19(a) correspond to the results of Ref. 65
 analyzing the 0.248 μm KrF laser radiation with the peak
 intensity of 10^8 – 10^9 W/cm², the pulse duration of 17 ns,
 and the spot size of 0.1×0.05 cm². In the experiment the
 target was rotated after every shot providing the shift of
 0.035 cm. The removed layer thickness was evaluated as
 $H_v = M(N\rho s)$, where M is the total removed mass determined
 by weighing, N is the number of shots, and ρ is the target
 density. Despite the plasma formation, the removed layer
 thickness grows monotonically with the increase in intensity.
 The numerical predictions, Fig. 19(a), solid line, have the
 same trend but are greater than experimental data by two to
 three times.

The alternative setup of experiment was used in Refs. 4
 and 55 for the 0.308 μm XeCl laser with the intensity range
 of 10^8 – 10^9 W/cm², the pulse duration of 20 ns, and the
 beam radius of 0.025 cm: the target was not rotated and the
 removed layer thickness per shot was calculated as the total
 depth of the hollow divided by the number of pulses. The
 obtained results were within a range of 0.1–1 μm, Fig.
 19(b), triangles, i.e., an order of magnitude higher than the
 results for the “rotational” setup, Figs. 19(a). The results pre-
 dicted numerically with the same laser parameters do not
 exceed 0.2 μm, Fig. 19(b), solid line. The predictions of the
 model in which the plasma effect was neglected are also
 shown by dashed line and, as it is seen, this curve lies much
 closer to the experimental dependence. This coincidence,
 however, is purely occasional and results from the codirec-
 tional effect of two factors: the contribution of the thermal
 evaporation greatly overestimated due to the neglected

858 plasma effect is compensated by the contribution of the non-
 859 thermal mechanism of removal in the experimental values.
 860 Summarizing, the comparison of numerical results with
 861 experimental data for the removed layer thickness demon-
 862 strated that the model correctly predicts trends for dependen-
 863 cies on radiation intensity, an accounting of the plasma effect
 864 is necessary for the correct estimation of the thermal mecha-
 865 nism contribution, and while analyzing experimental data on
 866 the UV laser radiation the other nonthermal mechanisms of
 867 removal have to be accounted for. One of the major reasons
 868 of the quantitative deviation is likely a great uncertainty of
 869 the target parameters used in the model at high temperature.

870 C. Dependence on the target material and 871 environment parameters

AQ: #2 872 The regularities considered in the previous sections are
 873 related to the laser irradiation of an aluminum target in
 874 vacuum. Below some qualitative considerations are pre-
 875 sented regarding to what extent these regularities can mani-
 876 fest themselves with other target materials and for the abla-
 877 tion in air or inert gas environment.

878 Numerical studies of the laser-induced phenomena in-
 879 volving the formation of vapor plasma often deal with only
 880 one material, e.g., aluminum^{30,32,37,41–43} or copper.^{23,28} It is
 881 explained by the complexity of calculation of the plasma
 882 properties, first of all its charge composition and absorption
 883 coefficient. Experimentally, the influence of the target mate-
 884 rial properties on laser evaporation and vapor plasma in-
 885 duced by the nanosecond Nd:YAG and ruby laser radiation
 886 with the intensity of about 10^9 W/cm² in vacuum was stud-
 887 ied in Refs. 17 and 46. It was established that the considered
 888 materials can be divided into two groups characterized by
 889 essentially different values of the threshold intensity of
 890 plasma formation, the thickness of the ablated layer as well
 891 as by the structure and the expansion regime of the plasma
 892 pattern. The explanation in Ref. 17 is that for the materials of
 893 the first group that includes Ti, Al, W, and some other metals
 894 the plasma is formed in the evaporated substance before the
 895 condition of thermodynamic instability $T > 0.9T_{\text{crit}}$ is reached
 896 on the surface. On the other hand, this condition is likely
 897 realized for the materials of the second group (Bi, Pb, Ge, Si)
 898 leading to the explosivelike decay of the overheated meta-
 899 stable phase⁵ and, consequently, to a much higher mass re-
 900 moval. Our numerical predictions for Al are consistent with
 901 the features of the first group (see Sec. III B), and thus one
 902 may suppose that the effect of the plasma on evaporation for
 903 other metals of the first group will be similar to the one
 904 established for aluminum for lasers operating in the near-IR
 905 and visible spectral range.

906 If laser ablation is performed in air or inert gas (He and
 907 Ar) environment at the typical pressure of 1 atm, the descrip-
 908 tion of the process becomes more complex and has to ac-
 909 count for the formation of the shock wave and plasma in the
 910 gas, diffusion, heat conduction, and recombination
 911 heating.^{51,69} From the point of view of the surface phase
 912 transition, the main distinction consists in the occasional for-
 913 mation of a second plasma in the environmental gas that
 914 might contribute to attenuation of the incident laser flux,
 915 generation of the counterpressure, and emission of the ther-

mal radiation. As a consequence, an accurate analysis of the
 phenomena has to be performed separately for every pair of
 the target material and environmental gas. The analysis of
 the Cu ablation in a chamber filled by He at the pressure of
 1 atm showed²³ that the principal characteristics of the sur-
 face (temperature, counter-pressure, direction of the phase
 transition, and removed layer thickness) are rather similar to
 the ones of this study and are controlled by the vapor plasma
 located in the near-surface region, while the plasma of He
 remains rather cold and transparent.

VI. CONCLUSION

The performed study allowed us to establish the follow-
 ing features of the phase transitions on the surface of an
 aluminum target and vapor plasma induced by the nanosec-
 ond radiation of the 1.06 and 0.248 μm lasers with the in-
 tensity of 10^8 – 10^9 W/cm².

- The 1.06 μm irradiation leads to the formation of an
 optically dense plasma with the temperature of
 5–10 eV that prevents further target heating. The
 evaporation stops but can occasionally resume at the
 final stage of the pulse. The evaporation proceeds non-
 uniformly in the spot area; the major contribution to
 mass removal occurs in the outer part of the spot
 above which the plasma is not formed and the sonic
 evaporation persists until the end of the action.
- The 0.248 μm laser plasma forms just at once after the
 beginning of the evaporation over all the spot area but
 remains colder and partially transparent transmitting
 30%–70% of the incident radiation; therefore the
 evaporation does not stop but continues in the sub-
 sonic regime with the Mach number of about 0.1 re-
 tardated by the high counterpressure of the near-surface
 plasma layer.
- For the 1.06 μm radiation, 15%–20% of the total of
 the evaporated matter condenses back to the surface
 during the laser pulse in consequence of the plasma
 counterpressure. For the UV radiation the condensa-
 tion is weaker, proceeds after the end of the pulses, the
 condensed fraction grows with the beam radius in-
 creasing but does not exceed 10%.
- For the beam radius smaller than ~ 100 μm the
 screening and retarding effect of the plasma weakens
 due to the lateral expansion, the thickness of the re-
 moved layer increases, and condensation after the end
 of the pulse does not occur.
- The structure, the shape, and the expansion regime of
 the plasma pattern induced by irradiation at different
 wavelengths have a number of distinctions; the contri-
 bution of the thermal plasma radiation and its effect on
 the target is much weaker than the ones of the laser
 radiation.
- The comparison of numerical and experimental data
 for the removed layer thickness demonstrated that the
 model correctly predicts trends for dependencies on
 radiation intensity and showed the importance of ac-
 counting for the plasma effect.

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